

## SECTION 2.7

## Absolute Value Functions and Graphs

### TRANSLATIONS OF FUNCTIONS

Vertical stretch of 5

Shift right 3 units

(when you take it out the parenthesis it changes the sign)

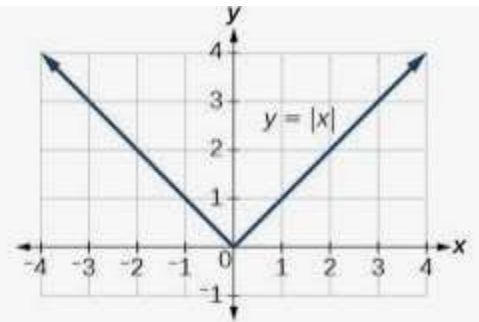
$$f(x) = -5(x-3)^2 + 7$$

Negative in front reflects across the x-axis

Shifts up 7 units

$f(x) = \sqrt{-x}$  means it reflects across the y-axis

### Absolute Value Graph



- 1) Make a table of values for the following equation. Then graph the equation.

$$y = |x| + 3$$

plug the x value of the table into  $y = |x| + 3$

Complete the table of values below.

x	y
-3	6
-1	4
0	3
1	4
3	6

$$|-3| + 3 = 6$$

$$|-1| + 3 = 4$$

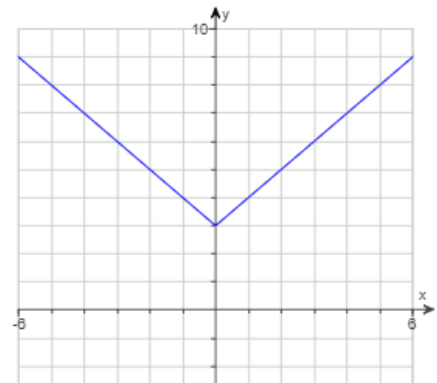
$$|0| + 3 = 3$$

$$|1| + 3 = 4$$

$$|3| + 3 = 6$$

(Simplify your answers.)

transformation is up 3 units



- 2) Make a table of values for the following equation. Then graph the equation.

$$y = |x+5|$$

plug the x value of the table into  $y = |x+5|$

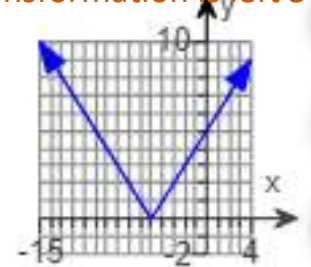
for EVERY x value in the table

Complete the table of values below.

x	y
-3	$ -3+5  = 2$
-1	$ -1+5  = 4$
0	$ 0+5  = 5$
1	$ 1+5  = 6$
3	$ 3+5  = 8$

$$|-3| + 3 = 6$$

transformation is left 5 units



- 3) Make a table of values for the following equation. Then graph the equation.

$$y = |x + 8|$$

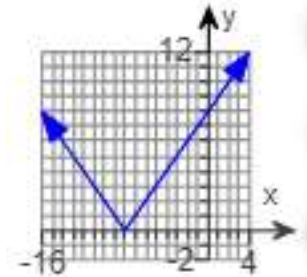
plug the x value of the table into  $y = |x + 8|$   
 for EVERY x value in the table

Complete the table of values below.

transformation is left 8 units

x	y
-3	$ -3 + 8  = 5$
-1	$ -1 + 8  = 7$
0	$ 0 + 8  = 8$
1	$ 1 + 8  = 9$
3	$ 3 + 8  = 11$

$$|-3 + 8| = 5$$



- 4) Make a table of values for the equation. Then graph the equation.

$$y = |x + 1| - 2$$

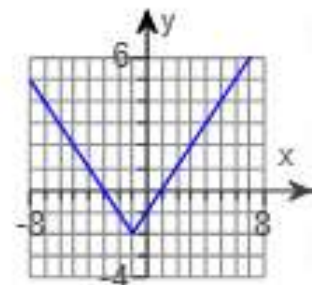
plug the x value of the table into  $y = |x + 1| - 2$   
 for EVERY x value in the table

Complete the table of values below.

transformation is left 1, down 3 units

x	y
-5	2
-3	0
-1	-2
0	-1
1	0
3	2
5	4

$$y = |-5 + 1| - 2 = 4 - 2 = 2$$



5) Make a table of values for the equation. Then graph the equation.

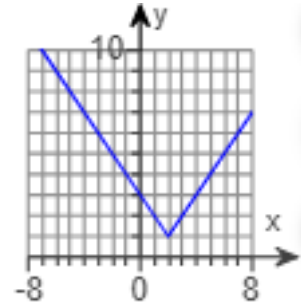
$$y = |x - 2| + 1$$

plug the x value of the table into  $y = |x - 2| + 1$   
for EVERY x value in the table

x	y
-5	8
-3	6
-1	4
0	3
1	2
3	2
5	4

$$y = |-5 - 2| + 1 = 7 + 1 = 8$$

transformation is left 1, down 3 units



6) Make a table of values for the following equation. Then graph the equation.

$$y = |x| + 4$$

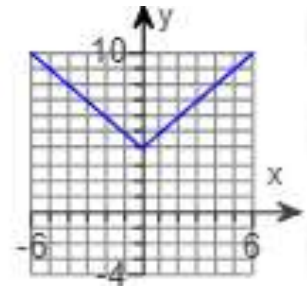
plug the x value of the table into  $y = |x| + 4$   
for EVERY x value in the table

Complete the table of values below.

x	y
-3	7
-1	5
0	4
1	5
3	7

$$y = |-3| + 4 = 3 + 4 = 7$$

transformation is up 4



7) Make a table of values for the following equation. Then graph the equation.

$$y = |x + 6|$$

plug the x value of the table into  $y = |x - 2| + 1$   
for EVERY x value in the table

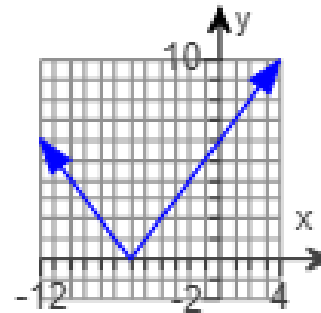
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Complete the table of values below.

transformation is left 6

x	y
-3	$ -3 + 6  = 3$
-1	$ -1 + 6  = 5$
0	$ 0 + 6  = 6$
1	$ 1 + 6  = 7$
3	$ 3 + 6  = 9$

$$y = |-3 + 6| = 3$$



8) Make a table of values for the following equation. Then graph the equation.

$$y = |x + 2|$$

plug the x value of the table into  $y = |x + 2|$   
for EVERY x value in the table

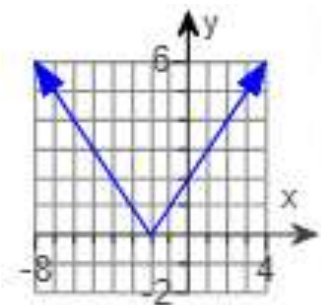
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Complete the table of values below.

transformation is left 2

x	y
-3	$ -3 + 2  = 1$
-1	$ -1 + 2  = 1$
0	$ 0 + 2  = 2$
1	$ 1 + 2  = 3$
3	$ 3 + 2  = 5$

$$y = |-3 + 2| = 1$$



9) Make a table of values for the equation. Then graph the equation.

$y = |x - 2| - 1$  plug the x value of the table into  $y = |x - 2| - 1$   
for EVERY x value in the table

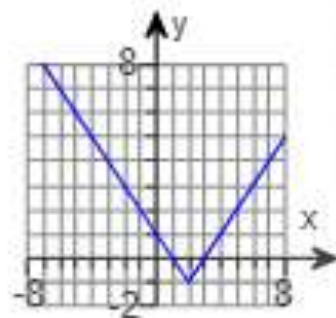
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Complete the table of values below.

x	y
-5	6
-3	4
-1	2
0	1
1	0
3	0
5	2

$y = |-5 - 2| - 1 = 7 - 1 = 6$

transformation is right 2, down 1



10) Make a table of values for the equation. Then graph the equation.

$y = |x + 3| + 5$  plug the x value of the table into  $y = |x + 3| + 5$   
for EVERY x value in the table

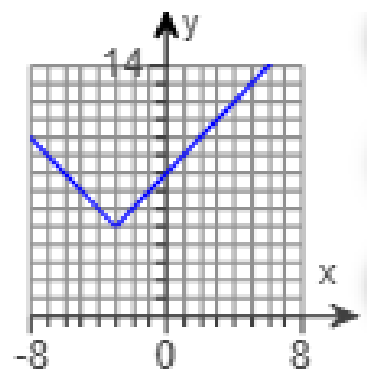
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Complete the table of values below.

x	y
-5	7
-3	5
-1	7
0	8
1	9
3	11
5	13

$y = |-5 + 3| + 5 = 2 + 5 = 7$

transformation is left 3, up 5



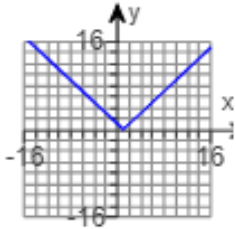
11) Sketch the graph of the function.

$$f(x) = |x| + 1$$

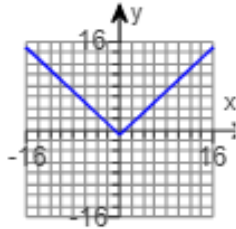
Shifts up 1

Choose the correct graph below.

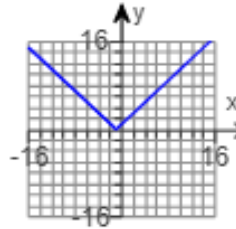
A.



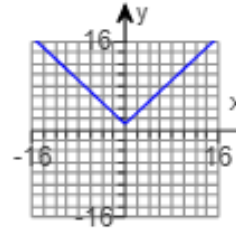
B.



C.



D.



12) Sketch the graph of the function.

$$f(x) = |x + 3|$$

Shifts up 1

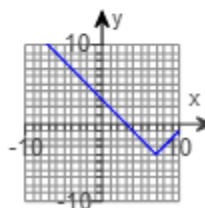
13) Find the graph of the function.

$$g(x) = |x + 7| - 4$$

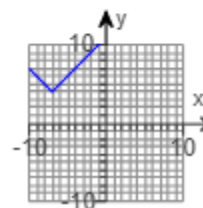
Shifts left 7 and down 4

Choose the correct graph below.

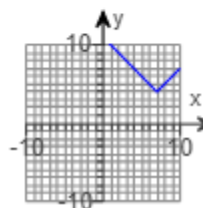
A.



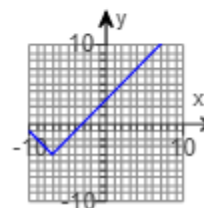
B.



C.



D.



14) Find the graph of the function.

$$g(x) = |x + 2| - 5$$

Shifts left 2 and down 5

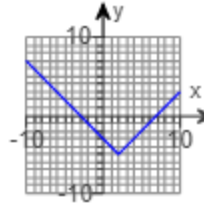
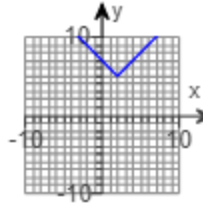
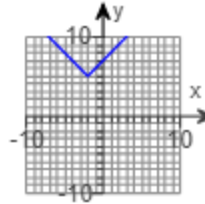
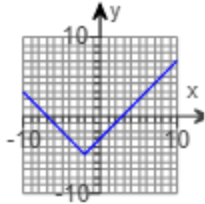
Choose the correct graph below.

A.

B.

C.

D.



15) Find the graph of the function.

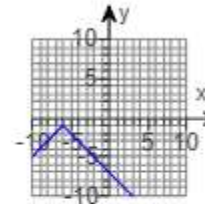
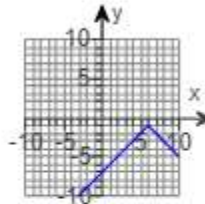
$$g(x) = -|x - 6| - 1$$

Reflects across the x-axis  
Shifts right 2 and down 1

Choose the correct graph below.

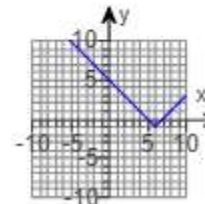
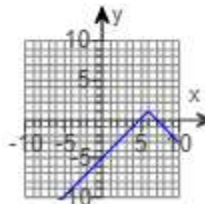
A.

B.



C.

D.



Find the graph of the function.

16)  $g(x) = |x + 5| - 4$

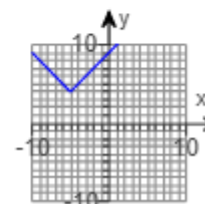
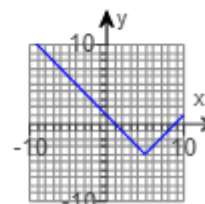
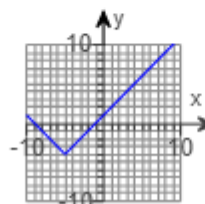
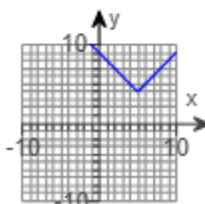
Choose the correct graph below. Shifts left 5 and down 4

A.

B.

C.

D.



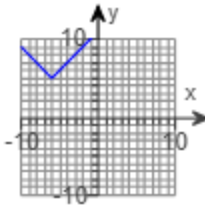
17) Find the graph of the function.

$$g(x) = |x + 6| - 5$$

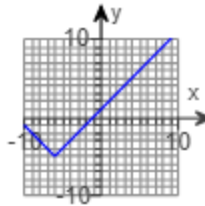
Choose the correct graph below.

Shifts left 6 and down 5

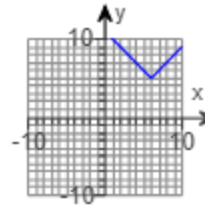
A.



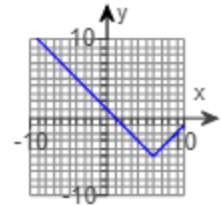
B.



C.



D.



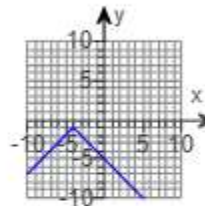
18) Find the graph of the function.

$$g(x) = -|x + 4| - 1$$

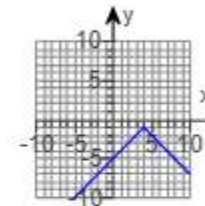
Reflects across the x-axis  
Shifts left 4 and down 1

Choose the correct graph below.

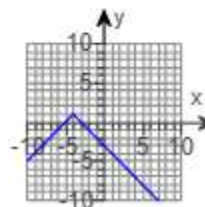
A.



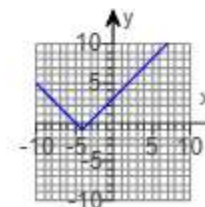
B.



C.



D.



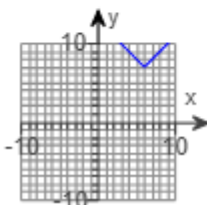
19) Find the graph of the function.

$$g(x) = |x + 6| - 7$$

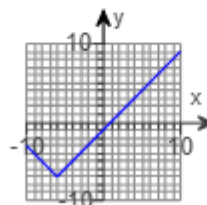
Choose the correct graph below.

Shifts left 6 and down 7

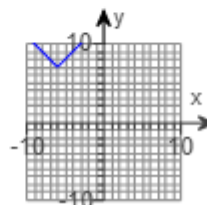
A.



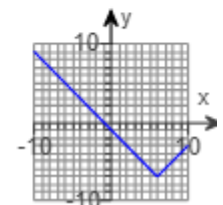
B.



C.



D.





20) Find the graph of the function.

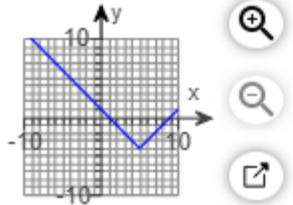
$$g(x) = |x + 5| - 4$$



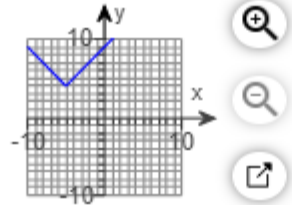
Choose the correct graph below.

Shifts left 5 and down 4

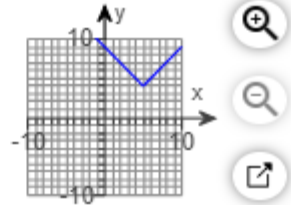
A.



B.



C.



D.

