

FUNCTIONS - OPERATIONS

- 1) Let $f(x) = 3x + 7$ and $g(x) = 2x^2$. Perform the function operation and then find the domain of the result.

$$(f + g)(x) \quad \text{add the two functions: } 3x + 7 + 2x^2$$

$$2x^2 + 3x + 7 \quad \text{Domain: all reals}$$

- 2) Let $f(x) = x - 3$ and $g(x) = 5x^2$. Perform the function operation and then find the domain of the result.

$$(f - g)(x) \quad \text{subtract the } g(x)$$

$$x - 3 - 5x^2 \quad \text{Put in order highest exponent first}$$

$$-5x^2 + x - 3 \quad \text{Domain: all reals}$$

- 3) Let $f(x) = 2x^2 + 5x - 7$ and $g(x) = x - 1$. Perform the function operation and then find the domain.

$$(f + g)(x) \quad \text{add the two functions: } 2x^2 + 5x - 7 + x - 1$$

$$\text{combine like terms and put in order} \quad 2x^2 + 6x - 8 \quad \text{Domain: all reals}$$

- 4) Let $f(x) = 3x^2 - 9x + 6$ and $g(x) = x - 2$. Perform the function operation and then find the domain of the result.

$$(f \cdot g)(x) \quad \text{multiply the two functions: } (3x^2 - 9x + 6)(x - 2)$$

$$\text{combine like terms and put in order} \quad 3x^3 - 9x^2 + 6x - 6x^2 + 18x - 12$$

$$3x^3 - 15x^2 + 24x - 12 \quad \text{Domain: all reals}$$

- 5) Let $f(x) = 3x + 5$ and $g(x) = x^2 - x + 3$. Perform the function operation and then find the domain.

$$f(x) + g(x) \quad \text{add the two functions: } 3x + 5 + x^2 - x + 3 \quad \text{combine like terms and put in order}$$

$$x^2 + 2x + 8 \quad \text{Domain: all reals}$$

- 6) Let $f(x) = 5x + 2$ and $g(x) = x^2 - x + 1$. Perform the function operation and then find the domain.

$$g(x) - f(x) \quad \text{subtract the right from the left function: } x^2 - x + 1 - (5x+2)$$

$$\text{combine like terms and put in order} \quad x^2 - x + 1 - 5x - 2$$

$$x^2 - 6x - 1 \quad \text{Domain: all reals}$$

- 7) Let $f(x) = 4x + 3$ and $g(x) = x^2 - 6x + 5$. Perform the function operation and then find the domain.

$$f(x) \cdot g(x) \quad \text{multiply the two functions: } (4x + 3)(3x^2 - 9x + 6)$$
$$12x^3 - 36x^2 + 24x + 9x^2 - 27x + 18$$
$$12x^3 - 27x^2 - 3x + 18 \quad \text{Domain: all reals}$$

- 8) Let $f(x) = 5x + 2$ and $g(x) = x^2 - 6x + 5$. Perform the function operation and then find the domain.

$$\frac{f(x)}{g(x)} \quad \text{divide the two functions * } g(x) \text{ on the bottom, do not simplify}$$
$$\frac{5x+2}{x^2-6x+5} \quad \text{**DOMAIN: CAN'T HAVE A ZERO IN DENOMINATOR}$$

Factor the bottom $(x-5)(x-1)$ DOMAIN: all reals except $x=5$ and $x=1$

- 9) Let $f(x) = 3x + 2$ and $g(x) = x^2 - 5x + 4$. Perform the function operation and then find the domain.

$$\frac{f(x)}{g(x)} \quad \text{divide the two functions * } g(x) \text{ on the bottom, do not simplify}$$
$$\frac{3x+2}{x^2-5x+4} \quad \text{**DOMAIN: CAN'T HAVE A ZERO IN DENOMINATOR}$$

Factor the bottom $(x-4)(x-1)$ DOMAIN: all reals except $x=4$ and $x=1$

- 10) Let $f(x) = x - 9$ and $g(x) = 3x^2$. Perform the function operation and then find the domain of the result.

$$(f + g)(x)$$

add the two functions: $x - 9 + 3x^2$ combine like terms and put in order

$$3x^2 + x - 9 \quad \text{Domain: all reals}$$

- 11) Let $f(x) = x - 6$ and $g(x) = x^2$. Perform the function operation and then find the domain of the result.

$$(f - g)(x)$$

subtract the left from the right function: $x - 6 - x^2$

Put in order highest exponent first $-x^2 + x - 6$ Domain: all reals

- 12) Let $f(x) = x^2 + 2x - 3$ and $g(x) = x - 1$. Perform the function operation and then find the domain.

$$(f + g)(x) \quad \text{add the two functions: } x^2 + 2x - 3 + x - 1 \text{ combine like terms and put in order}$$
$$x^2 + 3x - 4 \quad \text{Domain: all reals}$$

- 13) Let $f(x) = 3x^2 + 12x - 15$ and $g(x) = x + 5$. Perform the function operation and then find the domain of the result.

$(f \cdot g)(x)$ multiply the two functions: $(x + 5)(3x^2 + 12x - 15)$
 $3x^3 + \underline{12x^2} - 15x + \underline{5x^2} + 60x - 75$
 $3x^3 + 17x^2 + 45x - 75$ Domain: all reals

- 14) Let $f(x) = 4x + 3$ and $g(x) = x^2 - x + 4$. Perform the function operation and then find the domain.

$f(x) + g(x)$ add the two functions: $x^2 - x + 4 + 4x + 3$ combine like terms and put in order
 $x^2 + 3x + 7$ Domain: all reals

- 15) Let $f(x) = 5x + 4$ and $g(x) = x^2 - x + 3$. Perform the function operation and then find the domain.

$g(x) - f(x)$ subtract the left from the right function: $x^2 - x + 3 - (5x + 4)$
combine like terms and put in order
 $x^2 - x + 3 - 5x - 4$
 $x^2 - 6x - 1$ Domain: all reals

- 16) Let $f(x) = 3x + 2$ and $g(x) = x^2 - 9x + 20$. Perform the function operation and then find the domain.

$f(x) \cdot g(x)$ multiply the two functions: $(3x + 2)(x^2 - 9x + 20)$
 $3x^3 - \underline{27x^2} + 60x + \underline{2x^2} - 18x + 40$
 $3x^3 - 25x^2 + 42x + 40$ Domain: all reals

- 17) Let $f(x) = 5x + 4$ and $g(x) = x^2 - 6x + 5$. Perform the function operation and then find the domain.

$f(x) \cdot g(x)$ multiply the two functions: $(5x + 4)(x^2 - 6x + 5)$
 $5x^3 - \underline{30x^2} + 25x + \underline{4x^2} - 24x + 20$
 $5x^3 - 26x^2 + x + 20$ Domain: all reals

- 18) Let $f(x) = 5x + 4$ and $g(x) = x^2 - 8x + 15$. Perform the function operation and then find the domain.

divide the two functions * $g(x)$ on the bottom, do not simplify

$\frac{f(x)}{g(x)}$ $\frac{5x+4}{x^2-8x+15}$ **DOMAIN: CAN'T HAVE A ZERO IN DENOMINATOR

Factor the bottom $(x-5)(x-3)$ DOMAIN: all reals except $x=5$ and $x=3$

- 19) Let $f(x) = 2x + 5$ and $g(x) = x^2 - 3x + 2$. Perform the function operation and then find the domain.

$$\frac{f(x)}{g(x)}$$

divide the two functions * $g(x)$ on the bottom, do not simplify

$$\frac{2x+5}{x^2-3x+2}$$

****DOMAIN: CAN'T HAVE A ZERO IN DENOMINATOR**

Factor the bottom $(x-2)(x-1)$ **DOMAIN:** all reals except $x=2$ and $x=1$

- 20) Find a. $(f+g)(x)$ b. $(f+g)(6)$.

$$f(x) = 5x + 3, g(x) = 5x - 6 \text{ add the two functions: } 5x + 3 + 5x - 6$$

$$\text{combine like terms and put in order} \quad 10x - 3$$

$$\text{plug 6 in for } x: 10(6) - 3 = 57 \quad \text{Domain: all reals}$$

- 21) If $f(x) = x - 8$ and $g(x) = 4x^2$, find $(f+g)(x)$ and $(f+g)(4)$.

$$\text{add the two functions: } x - 8 + 4x^2 \text{ put in order} \quad 4x^2 + x - 8$$

$$\text{plug 4 in for } x: 4(4)^2 + (4) - 8 = 54 \quad \text{Domain: all reals}$$

- 22) Find a. $(f+g)(x)$ b. $(f+g)(7)$.

$$f(x) = 2x^2 - x - 2, g(x) = x - 3 \quad \text{add the two functions: } 2x^2 - x - 2 + x - 3$$

$$\text{combine like terms} \quad 2x^2 - 5$$

$$\text{plug 7 in for } x: 2(7)^2 - 5 = 93 \quad \text{Domain: all reals}$$

- 23) Let $f(x) = 5x$ and $g(x) = -2x - 6$. Find $(f+g)(x)$, $(f-g)(x)$, $(fg)(x)$, and $\left(\frac{f}{g}\right)(x)$.

$$5x - 2x - 6$$

$$(f+g)(x) = 3x - 6 \quad (\text{Simplify your answer.})$$

$$5x - (-2x - 6) = 5x + 2x + 6$$

$$(fg)(x) = -10x^2 - 30x \quad (\text{Simplify your answer.}) \quad 5x(-2x - 6)$$

$$\left(\frac{f}{g}\right)(x) = \frac{5x}{-2x - 6} \quad (\text{Simplify your answer.})$$

24) $f(x) = x^2 - 5x$ and $g(x) = 2 - x$

Find $(f+g)(x)$ and $(f+g)(7)$. add the two functions: $4x^2 - 5x + 2 - x$
combine like terms $4x^2 - 6x + 2$
plug 7 in for x: $4(7)^2 - 6(7) + 2 = 156$ Domain: all reals

25) Let $f(x) = x^2 - 5x$ and $g(x) = 7 + x$. Find $f(2) + g(2)$.

$$(2)^2 - 5(2) + 7 + (2) \\ -6 + 9 = 3$$

26) $f(x) = x^2 + 6x$ and $g(x) = 1 - x$

Find $(f-g)(x)$ and $(f-g)(3)$. subtract the left from the right function: $x^2 + 6x - (1 - x)$
combine like terms $x^2 + 5x + 1$
plug 4 in for x: $4(4)^2 + (4) - 8 = 54$ Domain: all reals

27) Let $f(x) = x^2 - 4x$ and $g(x) = 7 + x$. Find $f(-1) - g(-1)$.

$$(-1)^2 - 4(-1) - (7 + (-1)) \\ 5 - 6 = -1$$

28) Find a. $(f+g)(x)$ b. $(f+g)(8)$.

$f(x) = 5x + 4$, $g(x) = 4x + 3$ add the two functions: $5x + 4 + 4x + 3$
combine like terms $9x + 7$
plug 8 in for x: $9(8) + 7 = 79$ Domain: all reals